



Answer Key

MACHINE DESIGN

Refresher 02

$$\epsilon = \frac{\delta}{L}$$

$$0.0008 \frac{\text{in}}{\text{in}} = \frac{\delta}{(35\text{ft}) \left(\frac{12\text{in}}{1\text{ft}} \right)}$$

$$\delta = 0.335 \text{ in}$$

Length of Belt

$$L = \frac{\pi}{2} (D + d) + 2c + \frac{(D - d)^2}{4c}$$

$$= \frac{\pi}{2} (12'' + 7.5'') + 2(45'') + \frac{(12'' - 7.5'')^2}{4(45'')}$$

$$L = 120.7430 \text{ in}$$

$$L = 121 \text{ in}$$

SPEED OF The belt

$$v = \frac{\pi d N}{60} = \frac{\pi (7.5 \text{ in}) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right) (1700 \text{ rpm})}{60}$$

$$v = 55.6324 \text{ ft/sec}$$

Stress Concentration Factor

$$k_s = \frac{2c+1}{2c} ; c = \frac{D_m}{d} = \frac{D_o - d}{d}$$
$$= \frac{(9/16" - 0.090")}{0.090"}$$

$$c = 5.25$$

subst;

$$k_s = \frac{2(5.25)+1}{2(5.25)}$$

$$k_s = 1.0952$$

Bergstrasser Factor

$$k_B = \frac{4c + 2}{4c - 3} = \frac{4(5.25) + 2}{4(5.25) - 3}$$

$$k_B = 1.2778$$

6



Load of the beam

7



Shrink fit

8



Cape chisel

Pitch line Velocity

$$v = \frac{\pi D_1 N}{60} ; \text{ transverse Circular Pitch}$$

$$P_n = P \cos \phi$$

$$= \frac{12 \text{ teeth}}{\text{in}} \cos 30^\circ$$

$$P_n = 10.3923 \frac{\text{teeth}}{\text{in}}$$

and;

$$P = \frac{T_1}{D_1}$$

$$10.3923 = \frac{18}{D_1}$$

$$D_1 = 1.7320 \text{ in}$$

hence;

$$v = \frac{\pi (1.7320 \text{ in}) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right) (1500 \text{ rpm})}{60}$$

$$v = 11.3359 \text{ ft/sec}$$

transmitted load

$$Hp = \frac{F v}{33000}$$

$$1.8 \text{ hp} = \frac{F (11.3359 \text{ ft/sec}) \left(\frac{60 \text{ sec}}{1 \text{ min}} \right)}{33000}$$

$$F = 87.3332 \text{ lbs}$$

$$S_s = \frac{PD}{2t} = \frac{(160 \text{ lb/in}^2)(25 \text{ in})}{2(0.125 \text{ in})}$$

$$S_s = 16000 \text{ psi}$$

$$\delta = \frac{8Fc^3\eta}{dG}$$

$$0.5 \text{ in} = \frac{8(60 \text{ lbf})(6)^3(15)}{d(12 \times 10^6 \text{ lbf/in}^2)}$$

$$d = 0.2592 \text{ in}$$

mean diameter

$$C = \frac{D_m}{d}$$

$$6 = \frac{D_m}{0.2592 \text{ in}}$$

$$D_m = 1.5552 \text{ in}$$

14



Epicycloids

15



Contact ratio

16



20 deg

$$V_{rim} = b t \pi D \quad ; \quad \rho_{rim} = \frac{m}{V_{rim}}$$

$$\frac{m}{\rho_{rim}} = b t \pi D$$

Solving for the mass, m

$$\Delta E = \frac{F}{g_0} C_f (v_a^2)$$

$$v = \frac{\pi D N}{60} = \frac{\pi (6 \text{ ft}) (280 \text{ rpm})}{60}$$

$$v = 87.9646 \text{ ft/sec}$$

Subst;

$$2500 \text{ ft-lb} = \frac{F}{32.2 \text{ ft/sec}^2} (0.04) (87.9646 \text{ ft/sec})^2$$

$$F = m = 260.0878 \text{ lb}$$

Hence;

$$\frac{260.0878 \text{ lbs}}{0.260 \text{ lb/in}^3} = (12 \text{ in}) t \pi (6 \text{ ft}) \left(\frac{12 \text{ in}}{1 \text{ ft}} \right)$$

$$t = 0.3685 \text{ in}$$

Radius of Gyration

$$R = \sqrt{8.68 \times 10^{-4} (D_o^2 + D_i^2)} \quad ; \text{ ft}$$

$$= \sqrt{8.68 \times 10^{-4} [(24 \text{ in})^2 + (18 \text{ in})^2]}$$

$$R = 0.8839 \text{ ft}$$

Torque required

$$T = \frac{F R^2}{g_0} \left[\frac{2\pi (n_2 - n_1)}{60 t} \right]$$

$$= \frac{(220 \text{ lbs})(0.8839 \text{ ft})^2}{32.2 \text{ ft/sec}^2} \left[\frac{2\pi (220 - 160) \text{ rpm}}{60 (15 \text{ sec})} \right]$$

$$T = (2,235.9 \text{ ft-lb}) \left(\frac{12 \text{ in}}{1 \text{ ft}} \right)$$

$$T = 26,831.4 \text{ lb-in}$$

20



Melting

21



Babbitt

$$P = \frac{2\pi TN}{60} \quad ; \quad S_s = \frac{16T}{\pi d^3}$$

$$5800 \frac{\text{lb}}{\text{in}^2} = \frac{16T}{\pi (0.25 \text{ in})^3}$$

$$T = 17.7942 \text{ lb-in}$$

Subst:

$$P = \frac{2\pi (17.7942 \text{ lb-in}) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right) (2200 \text{ rpm})}{60}$$

$$P = \left(341.6237 \frac{\text{lb-ft}}{\text{sec}} \right) \left(\frac{1 \text{ hp}}{550 \frac{\text{lb-ft}}{\text{sec}}} \right)$$

$$P = 0.6211 \text{ hp}$$

$$\omega_{c1}(\text{shaft}) = 110 \text{ rad/sec}$$

$$\omega_{c2}(\text{pulley}) = 130 \text{ rad/sec}$$

$$\omega_{c3}(\text{gear}) = 125 \text{ rad/sec}$$

critical speed of the system

from: Dunkerley's Equation

$$\frac{1}{\omega_c^2} = \frac{1}{\omega_{c1}^2} + \frac{1}{\omega_{c2}^2} + \frac{1}{\omega_{c3}^2} + \dots + \frac{1}{\omega_{cn}^2}$$

$$\frac{1}{\omega_c^2} = \frac{1}{\left(110 \frac{\text{rad}}{\text{sec}}\right)^2} + \frac{1}{\left(130 \frac{\text{rad}}{\text{sec}}\right)^2} + \frac{1}{\left(125 \frac{\text{rad}}{\text{sec}}\right)^2}$$

$$\omega_c = 69.7044 \frac{\text{rad}}{\text{sec}}$$

Composition of forces

$$\begin{aligned}\Delta L &= \alpha L \Delta T \\ &= (6.5 \times 10^{-6})(12 \text{ in})(145 - 80) \text{ deg F} \\ \Delta L &= 5.07 \times 10^{-3} \text{ in}\end{aligned}$$

then;

$$S_s = E \frac{\delta}{L} = \left(30 \times 10^6 \frac{\text{lb}}{\text{in}^2} \right) \left(\frac{5.07 \times 10^{-3} \text{ in}}{12 \text{ in}} \right)$$

$$S_s = 12675 \frac{\text{lb}}{\text{in}^2}$$

$$\delta = \frac{PL}{AE}$$

$$\delta_{mm} = \frac{P(5000 \text{ mm})}{\frac{\pi(7 \text{ mm})^2}{4} (180 \times 10^3 \frac{\text{N}}{\text{mm}^2})}$$

$$P = 11083.5368 \text{ N}$$

27



Metal

$$\Delta E = \frac{F}{4g_0} (v_1^2 - v_2^2) \text{ for solid disc flywheel}$$

Peripheral speed

$$v_2 = v_1 - 0.12 v_1 = v_1 (1 - 0.12)$$

$$= 65 \frac{\text{ft}}{\text{sec}} (1 - 0.12)$$

$$v_2 = 57.2 \frac{\text{ft}}{\text{sec}}$$

$$v_1 = 65 \frac{\text{ft}}{\text{sec}}$$

Subst;

$$\Delta E = \frac{320 \text{ lbs}}{4 \left(32.2 \frac{\text{ft}}{\text{sec}^2} \right)} (65^2 - 57.2^2) \frac{\text{ft}^2}{\text{sec}^2}$$

$$\Delta E = 2368.0994 \text{ ft-lb}$$

Force Required to punch a hole

$$S_{sy} = \frac{F}{\pi D t}$$

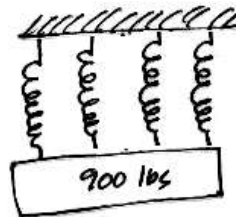
$$60000 \frac{\text{lb}}{\text{in}^2} = \frac{F}{\pi (1.5 \text{ in}) (3/4 \text{ in})}$$

$$F = 212\,057.5041 \text{ lbs}$$

30



5000/6000



$$k_1 = k_2 = k_3 = 45 \text{ lb/in}$$

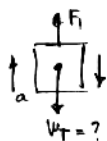
Deflection

$$k = \frac{P}{\delta}$$

$$45 \text{ lb/in} = \frac{900 \text{ lbs} / 4}{\delta}$$

$$\delta = 5 \text{ in}$$

FBD of the load

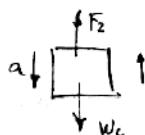


$$(\sum F_y = 0)$$

$$F_1 - W_T = m_T \left(\frac{a}{g_c} \right)$$

$$F_1 - W_T - m_T \left(\frac{a}{g_c} \right) = 0 \longrightarrow (1)$$

FBD of the counterweight



$$(\sum F_y = 0)$$

$$F_2 - W_c = -m_c \left(\frac{a}{g_c} \right)$$

$$F_2 - W_c + m_c \left(\frac{a}{g_c} \right) = 0 \longrightarrow (2)$$

from eq (2)

$$W_c = m_c \left(\frac{g_0}{g_c} \right)$$

$$m_c = W_c \left(\frac{g_c}{g_0} \right)$$

$$F_2 - W_c + W_c \left(\frac{a}{g_0} \right) = 0$$

$$F_2 - 3350 \text{ lb} + 3350 \text{ lb} \left(\frac{4 \text{ ft/sec}^2}{32.2 \text{ ft/sec}^2} \right)$$

$$F_2 = 2933.8509 \text{ lbs}$$

$$\text{from: } \frac{F_1}{F_2} = e^{f\theta}$$

$$F_1 = F_2 e^{f\theta} = F_2 e^{(0.3)(535^\circ) \left(\frac{\pi}{180^\circ} \right)}$$

$$F_1 = 2.5440 F_2 \longrightarrow (3)$$

from eq (3)

$$F_1 = 2.5440 (2933.8509 \text{ lbs})$$

$$F_1 = 7463.7168 \text{ lbs}$$

hence; from 1

$$F_1 - W_T - m_T \left(\frac{a}{g_c} \right) = 0$$

$$m_T = W_T \left(\frac{g_c}{g_0} \right)$$

$$F_1 - W_T - W_T \left(\frac{a}{g_0} \right) = 0$$

$$7463.7168 \text{ lbs} - W_T \left(1 + \frac{4 \text{ ft/sec}^2}{32.2 \text{ ft/sec}^2} \right) = 0$$

$$W_T = 6638.9967 \text{ lbs}$$

33



Machine

$$V = \pi D N$$

$$\left(1200 \frac{\text{ft}}{\text{min}}\right) \left(\frac{12 \cdot \text{in}}{1 \text{ ft}}\right) = \pi D (200 \frac{\text{ft}}{\text{min}})$$

$$D = 22.9183 \text{ in}$$

Thickness Required

$$S_s = \frac{PD}{2t} \quad ; \quad P = \gamma h$$

$$= \left(530 \frac{\text{kg}}{\text{m}^3} \right) \left(\frac{9.81 \frac{\text{m}}{\text{s}^2}}{1 \frac{\text{kg} \cdot \text{m}}{\text{N} \cdot \text{s}^2}} \right) (7 \text{ m})$$

$$P = 36,395.1 \frac{\text{N}}{\text{m}^2}$$

subst;

$$30 \times 10^6 \frac{\text{N}}{\text{m}^2} = \frac{(36,395.1 \frac{\text{N}}{\text{m}^2})(3.4 \text{ m})}{2t}$$

$$t = 2.0624 \times 10^{-3} \text{ m}$$

$$t = 2.0624 \text{ mm}$$

$$S_s = \frac{PD}{4tR}$$
$$65000 \frac{\text{lb}}{\text{in}^2} = \frac{P(14\text{in})}{4(\frac{1}{4}\text{in})(0.80)}$$

$$P = 3714.2857 \text{ psi}$$

37



Tempering

38



Reduce concentration factor

$$\alpha = \frac{\omega_2 - \omega_1}{t}$$
$$= \frac{(460 - 320) \frac{\text{rev}}{\text{min}} \left(\frac{1 \text{ min}}{60 \text{ sec}} \right) \left(\frac{360^\circ}{1 \text{ rev}} \right) \left(\frac{\pi \text{ rad}}{180^\circ} \right)}{38 \text{ sec}}$$

$$\alpha = 1.4881 \frac{\text{rad}}{\text{sec}^2}$$

40



Copper

Short shaft

$$P = \frac{D^3 N}{38} = \frac{(2.8 \text{ in})^3 (300 \text{ rpm})}{38}$$

$$P = 173.3053 \text{ hp}$$

Polar Section modulus

$$Z = 0.05 S^3$$

$$Z = 0.05 (4 \text{ in})^3$$

$$Z = 3.2 \text{ in}^3$$

Flange coupling

$$P = \frac{2\pi TN}{60}$$

$$27.5 \text{ kW} = \frac{2\pi T (450 \text{ rpm})}{60}$$

$$T = 0.5836 \text{ kN-m}$$

and;

$$\tau_s = \frac{2T}{\pi \left[\frac{\pi}{4} h^2 \right] N_b}$$

$$15 \times 10^3 \frac{\text{N}}{\text{m}^2} = \frac{2 (0.5836 \text{ kN-m})}{0.120 \text{ m} \left[\frac{\pi}{4} h^2 \right] 4}$$

$$h = 0.01436 \text{ m}$$

$$h = 14.36 \text{ mm}$$

$$\frac{\theta}{L} = \frac{T}{JG} ; \quad P = \frac{2\pi TN}{60}$$

$$(50 \text{ hp}) \left(\frac{550 \frac{\text{ft} \cdot \text{lb}}{\text{sec}}}{1 \text{ hp}} \right) = \frac{2\pi T (1300 \text{ rpm})}{60}$$

$$T = 202.00 \text{ lb} \cdot \text{ft}$$

$$J = \frac{\pi D^4}{32} = \frac{\pi \left[(1.50 \text{ in}) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right) \right]^4}{32}$$

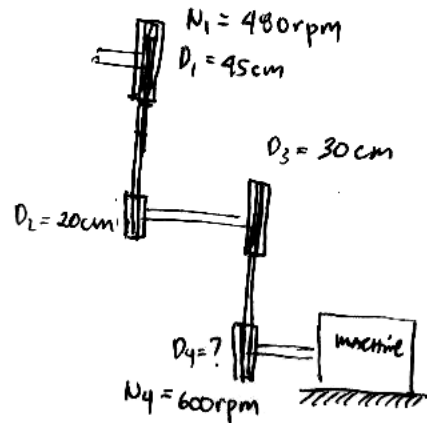
$$J = 2.3968 \times 10^{-5} \text{ ft}^4$$

Subst:

$$\frac{\theta}{L} = \frac{(202.00 \text{ lb} \cdot \text{ft})}{(2.3968 \times 10^{-5} \text{ ft}^4) \left(12.3 \times 10^6 \frac{\text{lb}}{\text{in}^2} \right) \left(\frac{144 \text{ in}^2}{1 \text{ ft}^2} \right)}$$

$$\frac{\theta}{L} = \left(4.758 \times 10^{-3} \frac{\text{rad}}{\text{ft}} \right) \left(\frac{180^\circ}{\pi \text{ rad}} \right)$$

$$\frac{\theta}{L} = 0.2726 \frac{\text{deg}}{\text{ft}}$$



$$D_1 N_1 = D_2 N_2$$

$$(45 \text{ cm})(480 \text{ rpm}) = (20 \text{ cm}) N_2$$

$$N_2 = 1080 \text{ rpm} = N_3$$

Then;

$$D_3 N_3 = D_4 N_4$$

$$(30 \text{ cm})(1080 \text{ rpm}) = D_4 (600 \text{ rpm})$$

$$D_4 = 54 \text{ cm}$$

$$P = \frac{D^3 N}{30} ; D = (40 \text{ mm}) \left(\frac{1 \text{ in}}{25.4 \text{ mm}} \right) = 1.5748 \text{ in}$$

$$N = \left(20 \frac{\text{rad}}{\text{sec}} \right) \left(\frac{60 \text{ sec}}{1 \text{ min}} \right) \left(\frac{180^\circ}{\pi \text{ rad}} \right) \left(\frac{1 \text{ rev}}{360^\circ} \right)$$

$$N = 190.9859 \text{ rpm}$$

Subst;

$$P = \frac{(1.5748 \text{ in})^3 (190.9859 \text{ rpm})}{30}$$

$$P = 19.6289 \text{ hp}$$

47



Class C

48



Ball bearing

$$\tau_s = \frac{16T}{\pi d^3} = \frac{16 (0.15 \text{ kN-m}) \left(\frac{1000 \text{ N}}{1 \text{ kN}} \right) \left(\frac{1000 \text{ mm}}{1 \text{ m}} \right)}{\pi (60 \text{ mm})^3}$$

$$\tau_s = 11.7893 \text{ MPa}$$

50



127

51



Equilibrium is maintained

52



Worm gear

53



UNC

54



Sprocket

$$S_s = \frac{16T}{\pi d^3} ; \quad P = \frac{2\pi TN}{60}$$

$$(80 \text{ hp}) \left(\frac{550 \frac{\text{lb-ft}}{\text{sec}}}{1 \text{ hp}} \right) = \frac{2\pi T (1900 \text{ rpm})}{60}$$

$$T = 221.1416 \text{ lb-ft}$$

Subst;

$$6500 \frac{\text{lb}}{\text{in}^2} = \frac{16 (221.1416 \text{ lb-ft}) \left(\frac{12 \text{ in}}{1 \text{ ft}} \right)}{\pi d^3}$$

$$d = 1.2763 \text{ in}$$

$$d = 1 - \frac{5}{16}''$$

Based on shear

$$S_s = \frac{2T}{dbL}$$

$$60 \frac{\text{N}}{\text{mm}^2} = \frac{2(1300 \text{ N-m})\left(\frac{1000 \text{ mm}}{1 \text{ m}}\right)}{(65 \text{ mm})(13 \text{ mm})L}$$

$$L = 51.2020 \text{ mm}$$

Based on tension

$$S_c = \frac{F_c}{A_c} ; T = F_c \left(\frac{d}{2} \right) ; A = \left(\frac{t}{2} \right) L$$

$$(1300 \text{ N-m}) \left(\frac{1000 \text{ mm}}{1 \text{ m}} \right) = F_c \left(\frac{65 \text{ mm}}{2} \right)$$

$$F_c = 40000 \text{ N}$$

Subst:

$$95 \frac{\text{N}}{\text{mm}^2} = \frac{40000 \text{ N}}{\left(\frac{15 \text{ mm}}{2} \right) (L)}$$

$$L = 56.1404 \text{ mm}$$

choose: 56.1404 mm

$$\theta = \frac{TL}{JG} \quad ; \quad S_s = \frac{16T}{\pi d^3}$$

$$T = \frac{\theta JG}{L} \quad ; \quad T = \frac{\pi S_s d^3}{16}$$

equating

$$\frac{\theta JG}{L} = \frac{\pi S_s d^3}{16} \quad ; \quad J = \frac{\pi d^4}{32}$$

$$\frac{\pi d^4 \theta G}{32 L} = \frac{\pi S_s d^3}{16}$$

$$d = \frac{2 S_s L}{\theta G}$$

Hence;

$$d = \frac{2 (75 \text{ N/mm}^2) (700 \text{ mm})}{(0.8 \text{ deg}) \left(\frac{\pi \text{ rad}}{180^\circ} \right) (75 \times 10^3 \frac{\text{N}}{\text{mm}^2})}$$

$$d = 100.2676 \text{ mm}$$

$$\theta = \frac{TL}{JG} ; \quad P = \frac{2\pi TN}{60}$$

$$60 \text{ kW} = \frac{2\pi T(480 \text{ rpm})}{60}$$

$$T = 1.1937 \text{ kN-m}$$

$$S_s = \frac{16T}{\pi d^3}$$

$$45 \times 10^3 \frac{\text{N}}{\text{m}^2} = \frac{16(1.1937 \text{ kN-m})}{\pi d^3}$$

$$d = 0.0513 \text{ m}$$

and from;

$$J = \frac{\pi d^4}{32} = \frac{\pi (0.0513 \text{ m})^4}{32} = 6.8053 \times 10^{-7} \text{ m}^4$$

hence;

$$\phi = \frac{(1.1937 \text{ kN-m})(12 \text{ m})}{(6.8053 \times 10^{-7} \text{ m}^4)(60 \times 10^6 \frac{\text{N}}{\text{m}^2})}$$

$$\phi = (0.2631 \text{ rad}) \left(\frac{180^\circ}{\pi \text{ rad}} \right)$$

$\phi = 15.0949 \text{ degrees.}$

$$S_s = \frac{16T}{\pi d^3} \quad ; \quad P = \frac{2\pi T N}{60}$$

$$25 \text{ kW} = \frac{2\pi T (720 \text{ rpm})}{60}$$

$$T = 0.3316 \text{ kN-m}$$

Subst;

$$S_s = \frac{16(0.3316 \text{ kN-m})}{\pi (0.030 \text{ m})^3}$$

$$S_s = 62549.0715 \text{ kPa}$$

$$S_s = \frac{16T}{\pi d^3} \quad ; \quad WP = Q \gamma T \Omega H$$

$$= \left(2000 \frac{\text{L}}{\text{min}}\right) \left(\frac{1 \text{ m}^3}{1000 \text{ L}}\right) \left(\frac{1 \text{ min}}{60 \text{ s}}\right) \left(9.81 \frac{\text{kN}}{\text{m}^3}\right) (14 \text{ m})$$

$$WP = 6.4092 \text{ kW}$$

and;

$$\eta_p = \frac{WP}{WP'}$$

$$0.70 = \frac{6.4092 \text{ kW}}{WP'}$$

$$WP' = 9.1560 \text{ kW}$$

from;

$$P = \frac{2\pi T N}{60}$$

$$9.1560 \text{ kW} = \frac{2\pi T (620 \text{ rpm})}{60}$$

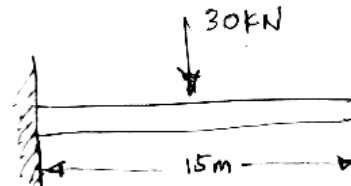
$$T = 0.1410 \text{ kN-m}$$

Hence;

$$S_s = \frac{16 (0.1410 \text{ kN-m})}{\pi (0.038 \text{ m})^3}$$

$$S_s = 13086.9497 \frac{\text{kN}}{\text{m}^2}$$

$$S_s = 13.08 \text{ MPa}$$



$$\theta = \frac{FL^2}{8EI} = \frac{(30 \text{ kN})(15 \text{ m})^2}{8(10000 \text{ kN-m}^2)}$$

$$\theta = 0.0844 \text{ rad}$$

62



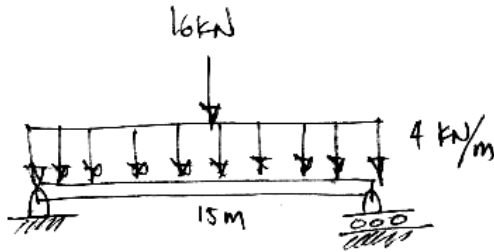
Silver-gray

63



80

Lateral deformation to the longitudinal deformation



Uniform load

$$y_1 = \frac{5WL^4}{384EI} = \frac{5(4\text{ kN/m})(15\text{ m})^4}{384(12,000\text{ kN-m})}$$

$$y_1 = 0.2197\text{ m}$$

concentrated load

$$y_2 = \frac{FL^3}{48EI} = \frac{(16\text{ kN})(15\text{ m})^3}{48(12000\text{ kN-m}^2)}$$

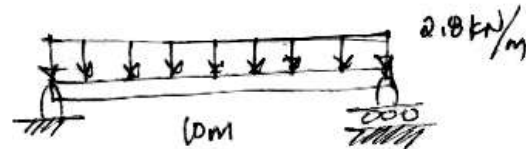
$$y_2 = 0.09375\text{ m}$$

Hence;

$$y_T = y_1 + y_2 = (0.2197 + 0.09375)\text{ m}$$

$$y_T = 0.3135\text{ m}$$

$$y_T = 313.45\text{ mm}$$

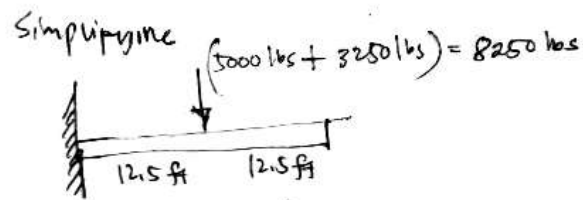
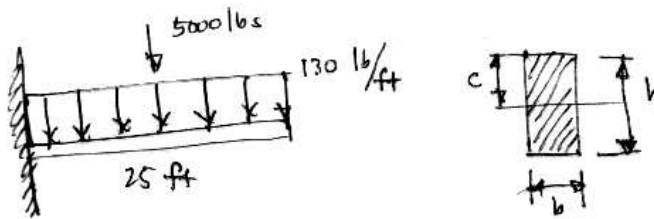


$$y = \frac{5WL^4}{384EI} = \frac{5(2.8 \text{ kN/m})(10 \text{ m})^4}{384(7200 \text{ kN-m}^2)}$$

$$y = 0.04521 \text{ m}$$

$$y = 45.21 \text{ mm}$$

67



$$S_f = \frac{Mc}{I} ; I = \frac{bh^3}{12} \quad (\text{for rectangular section})$$

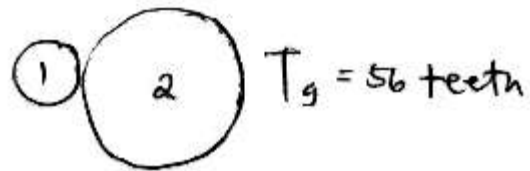
$$S_f = \frac{6M}{bh^2} \quad \text{psi}$$

$$M = (8250 \text{ lbs}) \left(12.5 \text{ ft} \right) \left(\frac{12 \text{ in}}{1 \text{ ft}} \right) = 1237500 \text{ lb-in}$$

Hence;

$$S_f = \frac{6 (1237500 \text{ lb-in})}{(9 \text{ in}) (12 \text{ in})^2}$$

$$S_f = 5729.1667 \text{ lb/in}^2$$



$$\frac{n_p}{n_g} = \frac{D_g}{D_p} = \frac{T_g}{T_p}$$

$$\frac{4}{1} = \frac{56 \text{ teeth}}{N_p}$$

$$T_p = 14 \text{ teeth}$$

$$T = f F_a \left[\frac{D^3 - d^3}{3(D^2 - d^2)} \right] N_c$$

$$= (0.30)(520 \text{ lbf}) \left[\frac{(9 \text{ in})^3 - (4.5 \text{ in})^3}{3(9^2 - 4.5^2)} \right] (1)$$

$$T = 691.6 \text{ lb-in}$$

Cone clutch

$$T = \frac{F_a f r_f}{\sin \theta} = \frac{(650 \text{ N})(0.40)(0.230/2 \text{ m})}{\sin 12^\circ}$$

$$T = 143.8111 \text{ N-m}$$

71



Dry

72



92xx

73



V-belt

cone clutch using uniform wear method

$$T = \frac{F_a f r_f}{\sin \phi} \quad ; \quad P = \frac{2\pi T N}{60}$$

$$10 \text{ kW} = \frac{2\pi T (550 \text{ rpm})}{60}$$

$$T = 0.1736 \text{ kN-m}$$

Subst;

$$0.1736 \text{ kN-m} = \frac{F_a (0.39) \left(\frac{0.30 \text{ m}}{2} \right)}{\sin 11^\circ}$$

$$F_a = 0.5662 \text{ kN}$$

$$F_a = 566.2 \text{ N}$$

75



Micrometer

$$S_t = \frac{F_1}{S_t b}$$

$$60 \text{ N/mm}^2 = \frac{8000 \text{ N}}{b(5 \text{ mm})}$$

$$b = 26.67 \text{ mm}$$

$$F_1 - F_2 = 5 \text{ kN}; \quad \frac{F_1}{F_2} = 4$$

$$F_1 = 4F_2$$

Subst,

$$4F_2 - F_2 = 5 \text{ kN}$$

$$F_2 = 1.6667 \text{ kN}$$

$$F_1 = 6.6668 \text{ kN}$$

$$F_1 = 3F_2$$

$$\frac{F_1}{F_2} = 3$$

$$\text{from; } \frac{F_1}{F_2} = e^{f\theta}$$

$$3 = e^{0.30 \theta}$$

$$\theta = (3.6620 \text{ rad}) \left(\frac{180^\circ}{\pi \text{ rad}} \right)$$

$$\theta = 209.8171 \text{ deg}$$

$$P = 2\pi TN ; T = (F_1 - F_2) r$$
$$= (5 \text{ kN}) \left(\frac{1.2 \text{ m}}{2} \right)$$
$$T = 3 \text{ kN-m}$$

subst;

$$P = \frac{2\pi (3 \text{ kN-m}) (320 \text{ rpm})}{60}$$

$$P = 100.5309 \text{ kW}$$

$$D = \frac{P}{\sin\left(\frac{180^\circ}{T}\right)}$$

$$28.654 \text{ in} = \frac{P}{\sin\left(\frac{180^\circ}{90}\right)}$$

$$P = 1.00 \text{ in}$$

$$D = \frac{P}{\sin\left(\frac{180^\circ}{T}\right)}$$

$$9.56 \text{ in} = \frac{\frac{1}{2} \text{ in}}{\sin\left(\frac{180^\circ}{T}\right)}$$

$$\sin\left(\frac{180^\circ}{T}\right) = 0.05236$$

$$\frac{180^\circ}{T} = 2.998^\circ$$

$$T = 60 \text{ teeth}$$

$$V = \frac{\pi DN}{60} = \frac{PTN}{60} = \frac{(3/4 \text{ in}) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right) (24) (620 \text{ rpm})}{60}$$

$$V = (15.5 \text{ ft/sec}) \left(\frac{60 \text{ sec}}{1 \text{ min}} \right)$$

$$V = 930 \text{ fpm}$$

$$D = \frac{P}{\sin\left(\frac{180^\circ}{T}\right)} = \frac{0.5 \text{ in}}{\sin\left(\frac{180^\circ}{20}\right)}$$

$$D = 3.1962 \text{ in}$$

Given: $600 \frac{\text{kN}}{\text{m}^2}$ per unit load

$$S_b = \frac{F}{bL} \quad ; \quad \frac{C_d}{D} = 0.0013$$

$$\frac{0.130 \text{ mm}}{D} = 0.0013$$

$$D = 100 \text{ mm}$$

Subst,

$$600 \frac{\text{kN}}{\text{m}^2} = \frac{30 \text{ kN}}{(0.1 \text{ m}) L}$$

$$L = 0.5 \text{ m}$$

$$L = 500 \text{ mm}$$

$$T_b = F f_b \frac{D}{2} ; F = \frac{60 \text{ kN}}{2} = 30 \text{ kN} \text{ load per bearing}$$

subst;

$$T_b = (30 \text{ kN}) (0.11) \left(\frac{0.22 \text{ m}}{2} \right)$$

$$T_b = 0.363 \text{ kN-m}$$

Hence;

$$P = \frac{2\pi T_b N}{60} = \frac{2\pi (0.363 \text{ kN-m}) (480 \text{ rpm})}{60}$$

$$P = 18.2464 \text{ kW}$$

$$T_b = F_f \frac{D}{2} = \left(\frac{4800 \text{ kg}}{2} \right) \left(\frac{9.81 \frac{\text{m}}{\text{s}^2}}{1 \frac{\text{kg} \cdot \text{m}}{\text{N} \cdot \text{s}^2}} \right) (0.20) \left(\frac{0.160 \text{ m}}{2} \right)$$

$$T_b = 376.704 \text{ N} \cdot \text{m}$$

Bearing stress

$$S_b = \frac{F}{bL} = \frac{\left(\frac{4500 \text{ kg}}{2}\right) \left(\frac{9.81 \frac{\text{m}}{\text{s}^2}}{1000 \frac{\text{kg} \cdot \text{m}}{\text{kN} \cdot \text{s}^2}}\right)}{(0.155 \text{ m})(0.290 \text{ m})}$$

$$S_b = 493.5456 \frac{\text{kN}}{\text{m}^2}$$

88



Left

89



Foundry

90



Newton's Law

91



Packings

$$C = \frac{D_1 + D_2}{2} ; P_d = \frac{T}{D}$$

$$D_1 = \frac{T_1}{P_d} = \frac{14 \text{ teeth}}{8} = 1.75 \text{ in}$$

$$D_2 = \frac{T_2}{P_d} = \frac{38 \text{ teeth}}{8} = 4.75 \text{ in}$$

Subst;

$$C = \frac{(1.75 + 4.75) \text{ in}}{2}$$

$$C = 3.25 \text{ in}$$

$$P = \frac{D^3 N}{80}$$
$$300 \text{ hp} = \frac{\left[(55 \text{ mm}) \left(\frac{1 \text{ in}}{25.4 \text{ mm}} \right) \right]^3 N}{80}$$

$$N = 2363.8739 \text{ rpm}$$

$$\text{Gear Ratio} = \frac{T_2}{T_1} = 4$$

$$C = 12 \text{ in}$$

$$T_2 = 64$$

$$P_c = \frac{\pi D}{T} ; \quad \frac{T_2}{T_1} = \frac{N_1}{N_2} ; \quad \frac{N_1}{N_2} = \frac{D_2}{D_1}$$

$$\frac{T_2}{T_1} = \frac{D_2}{D_1}$$

$$4 = \frac{D_2}{D_1}$$

$$D_2 = 4D_1$$

$$C = \frac{D_1 + D_2}{2}$$

$$12 \text{ in} = \frac{D_1 + 4D_1}{2}$$

$$D_1 = 4.8 \text{ in}$$

$$D_2 = 19.2 \text{ in}$$

Hence;

$$P_c = \frac{\pi D_2}{T_2} = \pi \left(\frac{19.2 \text{ in}}{64 \text{ teeth}} \right)$$

$$P_c = 0.9425 \text{ in/teeth}$$

$$W = S_t (0.55d^2 - 0.25d)$$

$$= 14\,000 \frac{\text{lb}}{\text{in}^2} [(0.55)(1.5 \text{ in})^2 - 0.25(1.5)]$$

$$W = 4\,278.75 \text{ lbs}$$

for 14.5° tooth thickness; $t = \frac{1.5708}{P_d}$

$$t = \frac{1.5708}{8 \text{ teeth/in}}$$

$$t = (0.19635 \text{ in}) \left(\frac{25.4 \text{ mm}}{1 \text{ in}} \right)$$

$$t = 4.9873 \text{ mm}$$

97



Hypoid

98



Allowance

99



Resilience

100



To sign plans, specifications, design etc.